

Explosive Ideas about Massive Stars – from Observations to Modeling Stockholm, AlbaNova University Center, August 10–13, 2011

### Modeling Core-Collapse Supernova Explosions

Is dimension a key to the neutrino mechanism?

Hans-Thomas Janka (Max Planck Institute for Astrophysics, Garching) THE ASTROPHYSICAL JOURNAL, 720:694-703, 2010 September 1 © 2010. The American Astronomical Society. All rights reserved. Printed in the U.S.A. doi:10.1088/0004-637X/720/1/694

#### DIMENSION AS A KEY TO THE NEUTRINO MECHANISM OF CORE-COLLAPSE SUPERNOVA EXPLOSIONS

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#### Collaborators

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**Ewald Müller** 

### Outline

- Moving to the 3<sup>rd</sup> dimension: A really grand computational challenge
- Status of modeling neutrino-driven explosions in 2D
- The 3<sup>rd</sup> dimension as a key to the neutrino mechanism:
   Do we understand how the key fits into the keyhole?
- 3D models on their way to meet observations

### Outline – Reversed

- 3D models on their way to meet observations
- Moving to the 3<sup>rd</sup> dimension: A really grand computational challenge
- Status of modeling neutrino-driven explosions in 2D
- The 3<sup>rd</sup> dimension as a key to the neutrino mechanism: Do we understand how the key fits into the keyhole?

#### Observational Consequences and Implications of Neutrino Heating and SASI in Stellar Explosions

- Neutron star kicks (Scheck et al. 2004, 2006; Wongwathanat et al. 2010)
- Asymmetric mass ejection & large-scale radial mixing (Kifonidis et al. 2005, Hammer er al. 2010)
- Characteristic neutrino-signal modulations
   (Marak et al. 2000; Müller et al. 2

(Marek et al. 2009; Müller et al. 2011)

Gravitational-wave signals

(Marek et al. 2009; Müller et al. 2011)

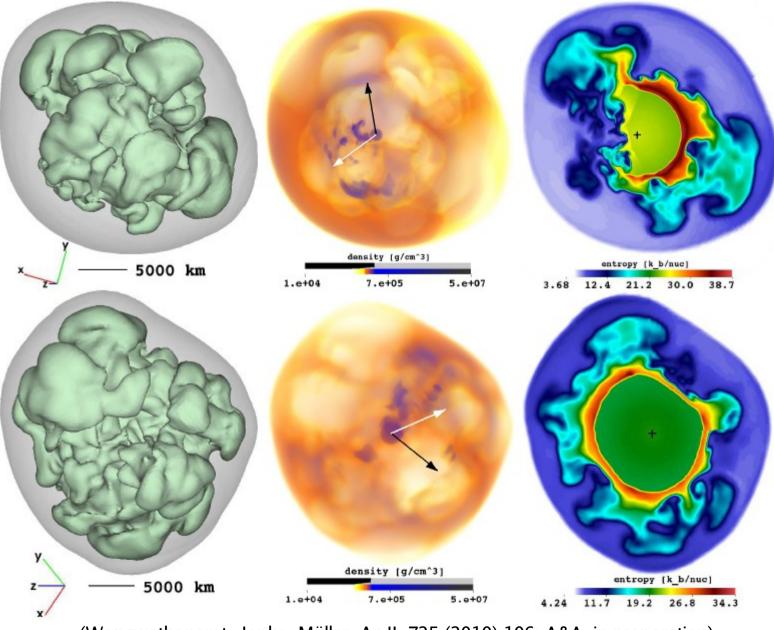
See Ewald Müller's talk on Saturday !

# Neutron Star Kicks in 3D Explosions

Parametric explosion calculations:

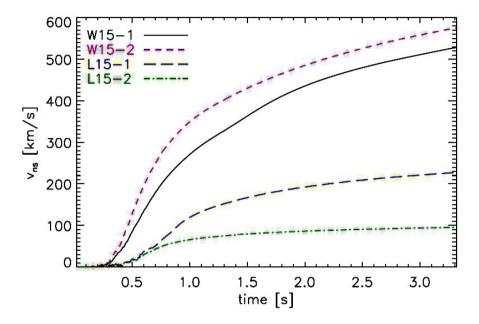
Neutrino core luminosity of proto-NS chosen; Accretion luminosity calculated with simple (grey) transport scheme.

#### Neutron Star Recoil in 3D



(Wongwathanarat, Janka, Müller, ApJL 725 (2010) 106; A&A, in preparation)

#### Neutron Star Recoil in 3D



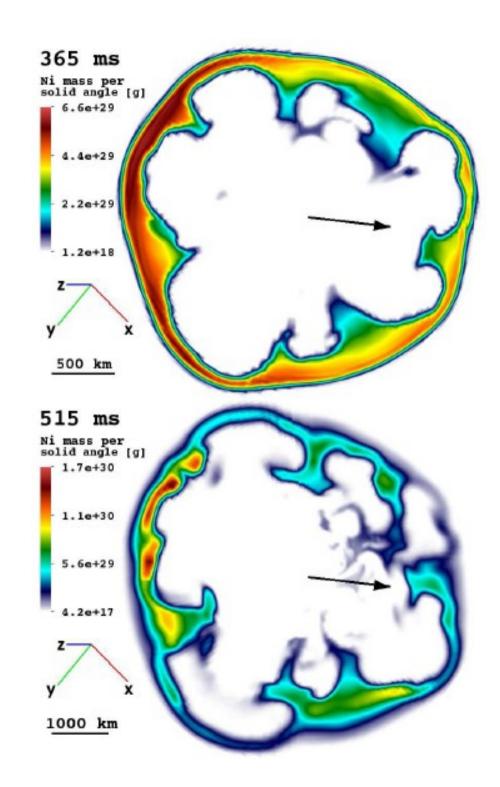
(Wongwathanarat, Janka, Müller, ApJL 725 (2010) 106; A&A, in preparation)

Model	$M_{\rm ns}$ [ $M_{\odot}$ ]	t <sub>exp</sub> [ms]	$E_{exp}$ [B]	v <sub>ns</sub> [km/s]	$a_{\rm ns}$ [km/s <sup>2</sup> ]	$v_{ns,v}$ [km/s]	$\alpha_{k\nu}$ [°]	v <sup>long</sup> [km/s]	$a_{ns}^{long}$ [km/s <sup>2</sup> ]	$J_{\rm ns,46}$ [10 <sup>46</sup> g cm <sup>2</sup> /s]	$\alpha_{sk}$	$T_{\rm spin}$ [ms]
W15-1	1.37	246	1.12	331	175	3	151	525	44	1.51	117	652
W15-2	1.37	248	1.13	405	144	1	126	575	49	1.56	58	632
W15-3	1.36	250	1.11	266	126	1	160	-	-	1.13	105	864
W15-4	1.38	272	0.94	262	136	4	162	-	-	1.27	43	785
W15-5-lr	1.40	270	0.97	128	72	1	102	-	-	2.29	141	440
L15-1	1.58	421	1.13	161	66	5	135	228	16	1.89	148	604
L15-2	1.51	381	1.74	78	3	1	150	96	4	1.04	62	1041
L15-3	1.62	477	0.84	31	0	1	51	-	-	1.55	123	750
L15-4-lr	1.70	703	0.55	146	152	4	62	-	-	1.64	100	743
N20-1-lr	1.53	348	0.83	175	62	30	171	-	-	2.81	155	393
N20-2	1.28	265	3.12	101	1	4	159	-	-	7.26	43	127

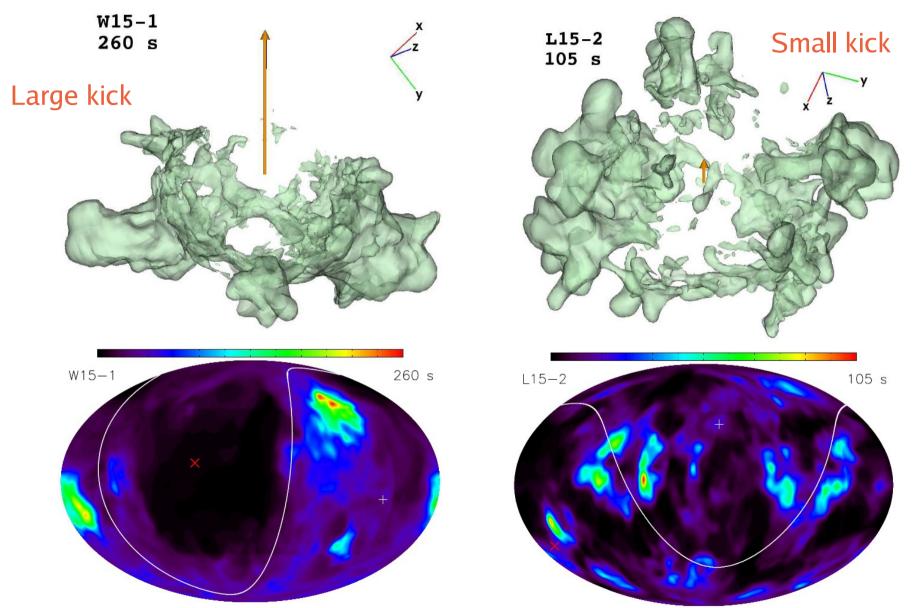
Neutron Star Recoil and Nickel Production

Nickel production is enhanced in direction of stronger explosion, i.e. opposite to NS kick

> (Wongwathanarat, Janka, Müller, A&A, to be submitted)



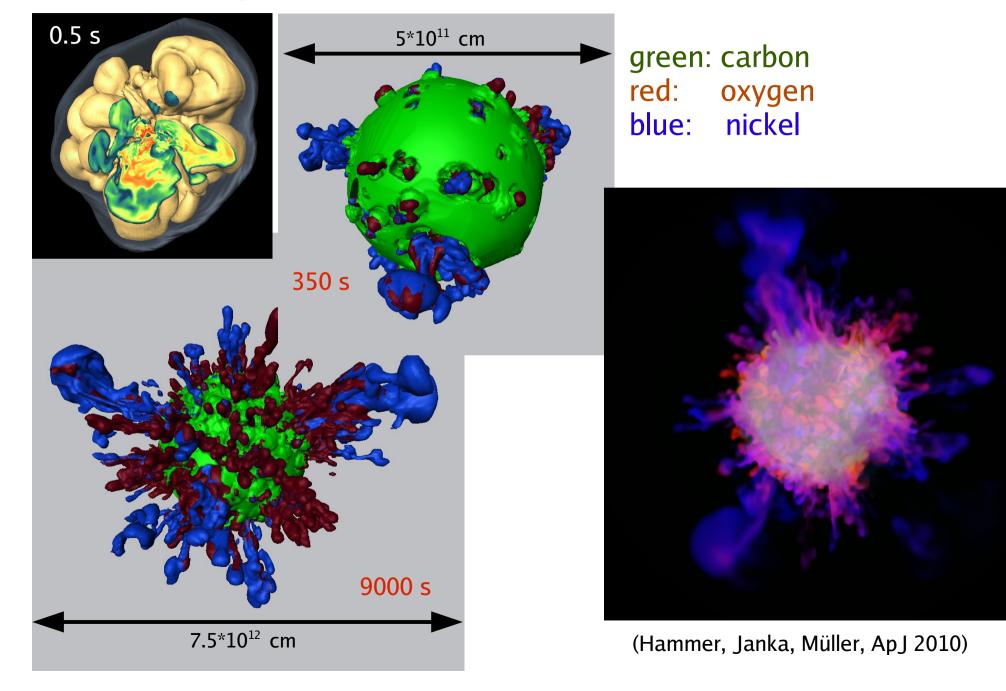
#### Neutron Star Recoil and Nickel Production



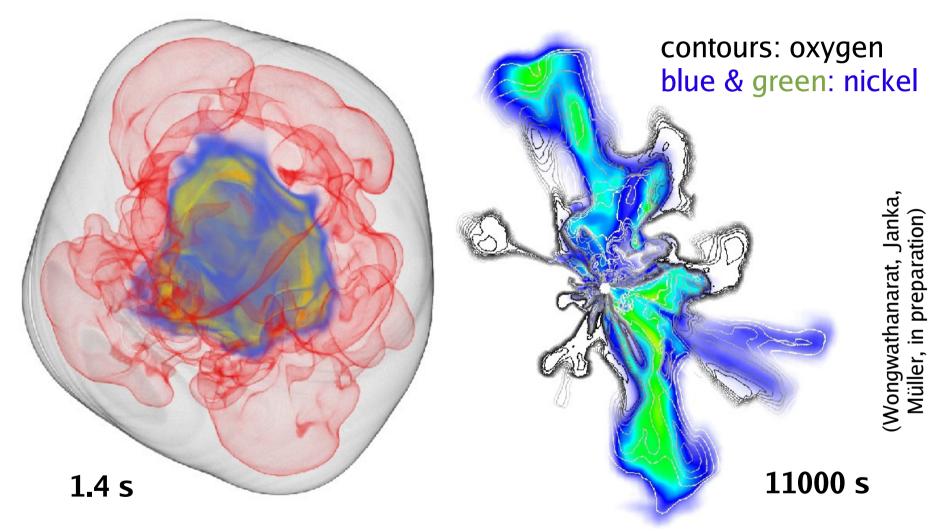
Enhanced concentration of iron in supernova remnants opposite to direction of large pulsar kick can be observable consequence of hydrodynamical kick mechanism.

3D Explosions and Supernova Asymmetries

#### Mixing Instabilities in 3D SN Models

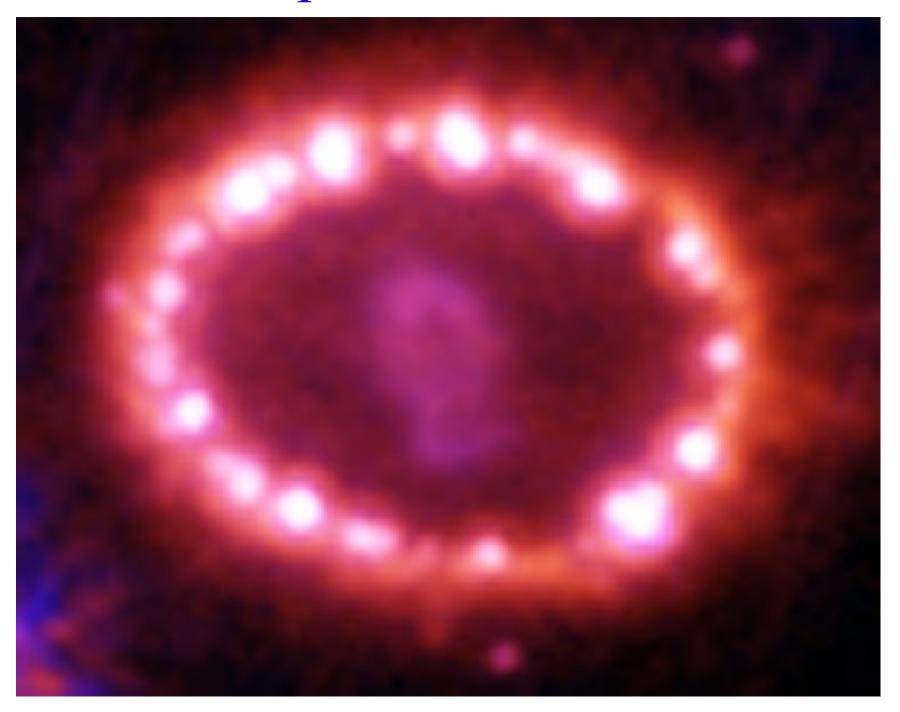


### Asymmetry of Supernova 1987A



Relatively small convective asymmetries of early explosion can grow into largescale asymmetry of the nickel and heavy-elements distributions!

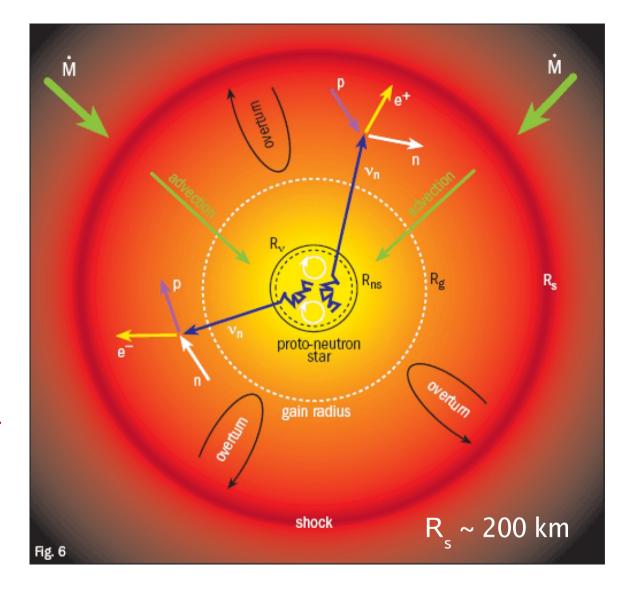
# Supernova 1987A



# BUT: Do We Understand How It All Starts?

Neutrinos & Explosion Mechanism

Paradigm: Explosions by the convectively supported neutrinoheating mechanism



- "Neutrino-heating mechanism": Neutrinos `revive' stalled shock by energy deposition (Colgate & White 1966, Wilson 1982, Bethe & Wilson 1985);
- Convective processes & hydrodynamic instabilities enhance the heating mechanism (Herant et al. 1992, 1994; Burrows et al. 1995, Janka & Müller 1994, 1996; Fryer & Warren 2002, 2004; Blondin et al. 2003; Scheck et al. 2004,06,08).

#### Neutrino Heating and Cooling

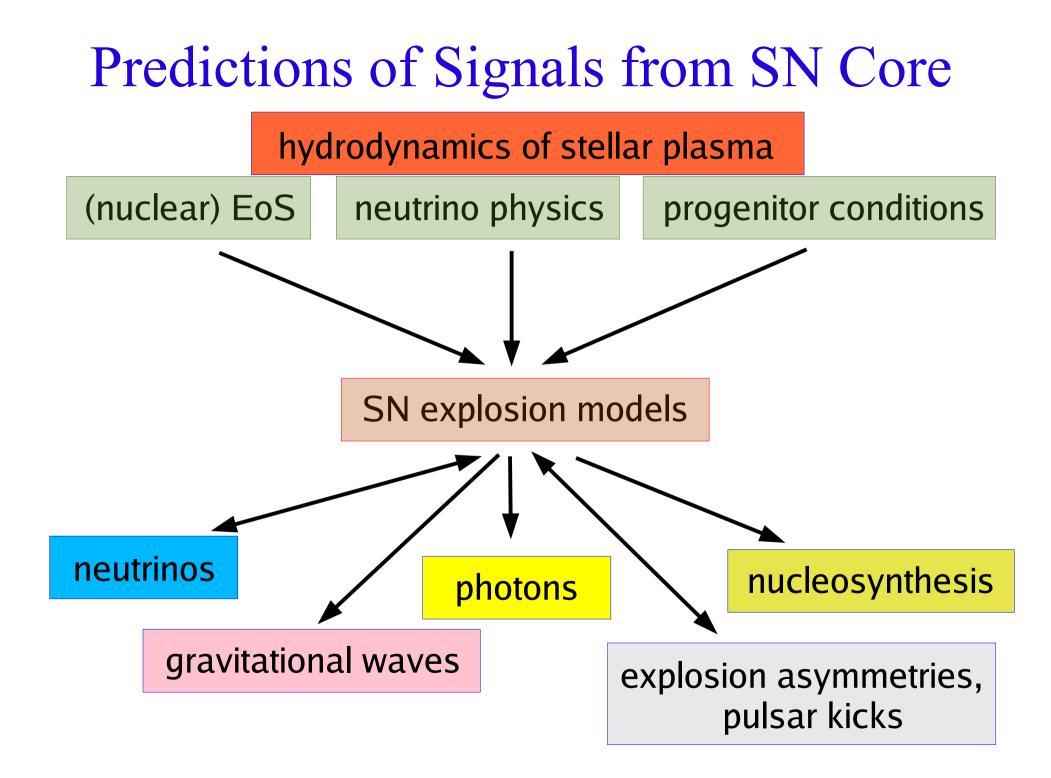
• Neutrino heating:

$$\mathcal{H} = 1.544 \times 10^{20} \left( \frac{L_{\nu_e}}{10^{52} \text{ erg s}^{-1}} \right) \left( \frac{T_{\nu_e}}{4 \text{ MeV}} \right)^2 \times \left( \frac{100 \text{ km}}{r} \right)^2 (Y_n + Y_p) \qquad \left[ \frac{\text{erg}}{\text{g s}} \right]$$

• Neutrino cooling:

$$C = 1.399 \times 10^{20} \left(\frac{T}{2 \text{ MeV}}\right)^6 (Y_n + Y_p) \qquad \left[\frac{\text{erg}}{\text{g s}}\right]$$

Multi-Dimensional Modeling as Computational Challenge



$$\frac{\partial\sqrt{\gamma}\rho W}{\partial t} + \frac{\partial\sqrt{-g}\rho W^{2}}{\partial t} = 0, \quad (2.5)$$

$$\frac{\partial\sqrt{\gamma}\rho W^{2}}{\partial t} + \frac{\partial\sqrt{-g}(\rho W^{2}_{29}i + \delta_{1}^{2})}{\partial x^{4}} = \frac{1}{2}\sqrt{-g}T^{\mu\nu}\frac{\partial g_{\mu\nu}}{\partial g_{2}i} + \left(\frac{\partial\sqrt{\gamma}\gamma}{\partial t}\right)_{C}, \quad (2.6)$$

$$\frac{\partial\sqrt{\gamma}\rho WY_{e}}{\partial t} + \frac{\partial\sqrt{-g}(\tau^{0} + Pv^{1})}{\partial x^{4}} = \alpha\sqrt{-g}\left(T^{\mu0}\frac{\partial \ln a}{\partial x^{\mu}} - T^{\mu\nu}\Gamma_{\mu\nu}^{0}\right) + \left(\frac{\partial\sqrt{\gamma}\tau}{\partial t}\right)_{C}, \quad (2.7)$$

$$\frac{\partial\sqrt{\gamma}\rho WY_{e}}{\partial t} + \frac{\partial\sqrt{-g}\rho WY_{e}^{0}i}{\partial x^{4}} = \left(\frac{\partial\sqrt{\gamma}\rho WY_{e}}{\partial t}\right)_{C}, \quad (2.8)$$

$$\frac{\partial\sqrt{\gamma}\rho WY_{e}}{\partial t} + \frac{\partial\sqrt{-g}\rho WY_{e}^{0}i}{\partial x^{4}} = 0. \quad (2.9)$$

$$\frac{\partial\sqrt{\gamma}\rho WX_{e}}{\partial t} + \frac{\partial\sqrt{-g}\rho WY_{e}^{0}i}{\partial x^{4}} = 0. \quad (2.9)$$

$$\frac{\partial\sqrt{\gamma}\rho WX_{e}}{\partial t} + \frac{\partial\sqrt{-g}\rho WY_{e}^{0}i}{\partial x^{4}} = 0. \quad (2.10)$$

$$\frac{\partial\sqrt{\phi}}{\partial t} + \frac{\partial\sqrt{-g}\rho WX_{e}^{0}i}{\partial x^{4}} = 0. \quad (2.9)$$

$$\frac{\partial\sqrt{\phi}}{\partial t} + \frac{\partial\sqrt{\gamma}}{\partial t} + \frac{\partial\sqrt{-g}\rho WY_{e}^{0}i}{\partial x^{4}} = 0. \quad (2.10)$$

$$\frac{\partial\sqrt{\phi}}{\partial t} + \frac{\partial\sqrt{\gamma}}{\partial t} + \frac{\partial\sqrt{\gamma}}{\partial x^{4}} = 0. \quad (2.9)$$

$$\frac{\partial\sqrt{\phi}}{\partial t} + \frac{\partial\sqrt{\gamma}}{\partial t} + \frac{\partial\sqrt{\gamma}}}{\partial t} +$$

#### Neutrino Reactions in Supernovae

Beta processes:

Neutrino scattering:

Thermal pair processes:

Neutrino-neutrino reactions:

•  $e^- + p \rightleftharpoons n + v_e$ 

• 
$$e^+ + n \rightleftharpoons p + \bar{v}_e$$

- $e^- + A \rightleftharpoons v_e + A^*$
- $v + n, p \rightleftharpoons v + n, p$
- $\nu + A \rightleftharpoons \nu + A$
- $\nu + e^{\pm} \rightleftharpoons \nu + e^{\pm}$
- $N+N \rightleftharpoons N+N+\nu+\bar{\nu}$

• 
$$e^+ + e^- \rightleftharpoons v + \bar{v}$$

- $v_x + v_e, \bar{v}_e \rightleftharpoons v_x + v_e, \bar{v}_e$  $(v_x = v_\mu, \bar{v}_\mu, v_\tau, \text{ or } \bar{v}_\tau)$
- $v_e + \bar{v}_e \rightleftharpoons v_{\mu,\tau} + \bar{v}_{\mu,\tau}$

# The Curse and Challenge of the Dimensions

Boltzmann equation determines neutrino distribution function in phase space

 $f(r, \theta, \phi, \Theta, \Phi, \epsilon, t)$ 

Integration over momentum space yields source terms for hydrodynamics

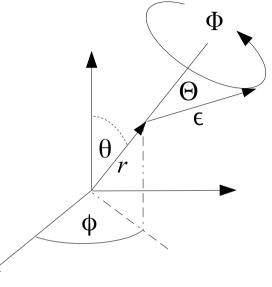
 $Q(r, \theta, \phi, t)$ ,  $\dot{Y}_e(r, \theta, \phi, t)$ 

#### Solution approach

- **3D** hydro + **6D** direct discretization of Boltzmann Transport Equation (no serious attempt yet)
- **2D** hydro + **5D** direct discretization of Boltzmann transport Equation (only with reduced complexity)

#### • **2D** hydro + "**ray-by-ray-plus**" variable Eddington factor method (current method of MPA)

• **3D** hydro + "**ray-by-ray-plus**" variable Eddington factor method (current method of MPA)



#### Required resources

- $\geq$  1–10 Pflops/s (sustained!)
- $\geq$  10–100 Tflops/s, TBytes
- $\geq 0.1-1$  Tflops/s, < 1 Tbyte
- $\geq$  10–100 Tflops/s, TBytes

# Computing requirements for 2D & 3D SN modeling

**Time-dependent simulations:**  $t \sim 1$  second,  $\sim 10^6$  time steps!

CPU-time requirements for one model run:

In 2D with 600 radial zones, 1 degree lateral resolution:

~ 3\*10<sup>18</sup> Flops, need ~3 years on 32 processor cores

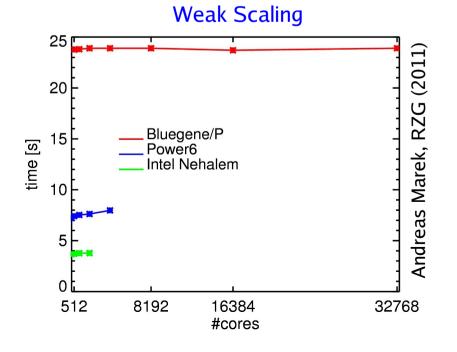
In 3D with 600 radial zones, 1.5 degrees angular resolution:

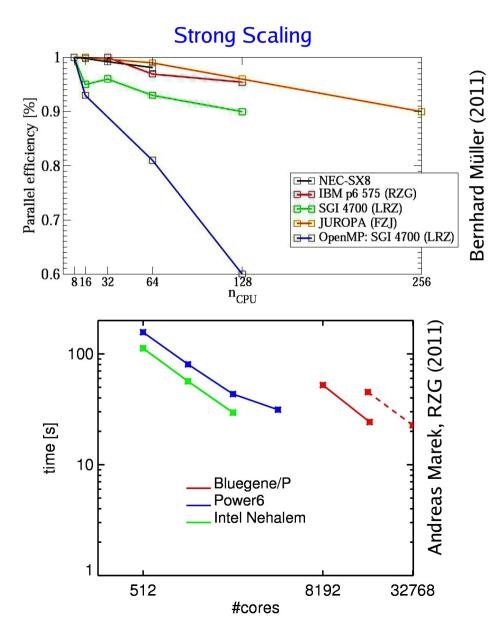
~ 3\*10<sup>20</sup> Flops, need ~1.5 years on 8192 processor cores



#### Performance and Portability of our Supernova Code *Prometheus-Vertex*

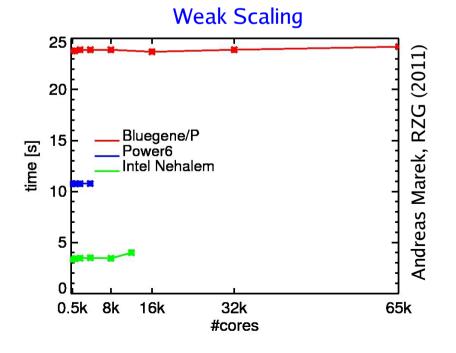
- Code employs hybrid MPI/OpenMP programming model.
- Code is portable to different computer platforms.
- Code shows excellent parallel efficiency, which will be fully exploited in 3D.

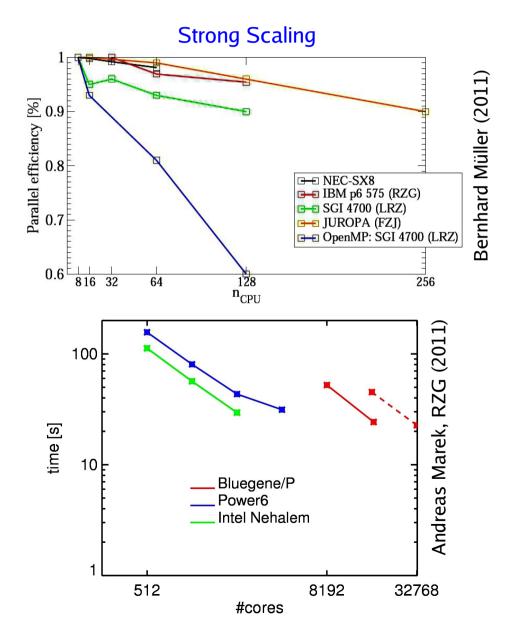




#### Performance and Portability of our Supernova Code *Prometheus-Vertex*

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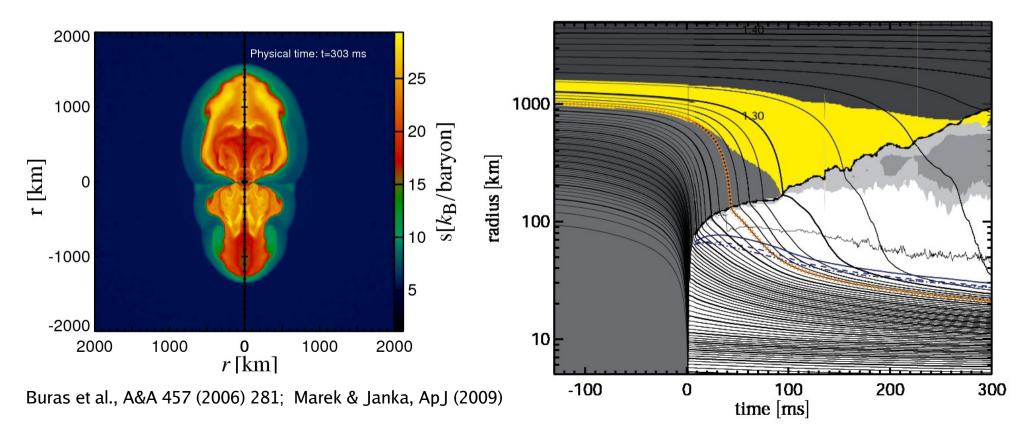
Results of 2D Simulations

# 2D SN Simulations: $M_{star} \sim 11 M_{sun}$

Nonradial hydrodynamic instabilities are crucial for the explosion !

Low-order (dipole, I=1, and quadrupole, I=2) modes of the "standing accretion shock instability" ("SASI"; Blondin et al. 2003) cause asymmetries and push shock to larger radii

==> This stretches residence time of matter in neutrino heating layer and thus increases energy absorbed by matter from neutrinos. Leads to initiation of globally aspherical explosion even without rotation





40

30

20

10

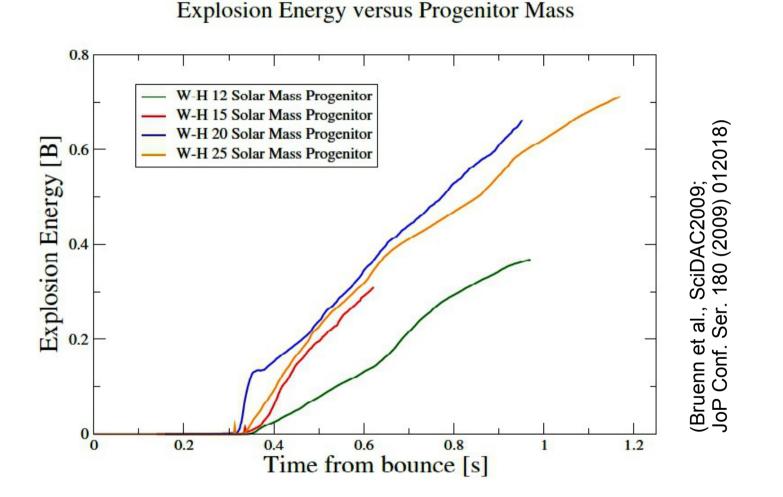
400

200

s[kB/baryon]

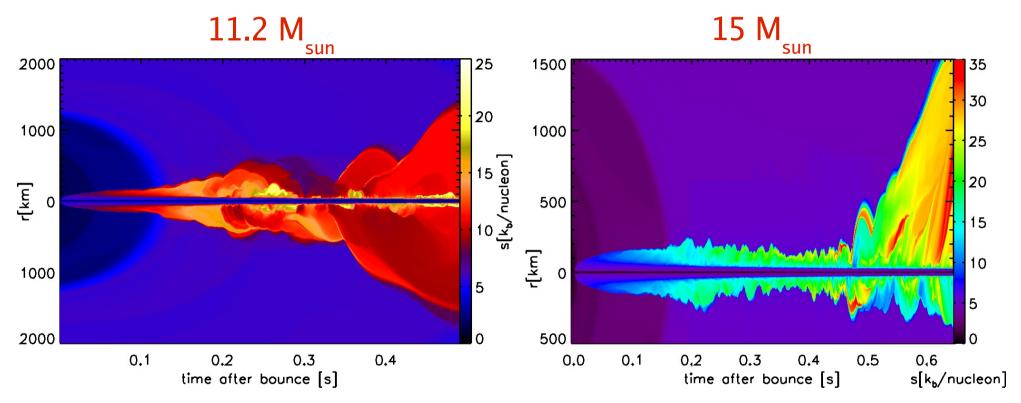
400 Violent SASI oscillations: Physical time: t=610 ms v-driven explosion sets in 200 at t ~ 600 ms after bounce r [km] 0 -200 1000 -400 radius [km] 400 200 0 r [km] 100 (Marek, PhD Thesis 2007; Marek & THJ, ApJ, 2009) 10 -200 200 400 600 0 time [ms]

### Explosions by Oak Ridge Group



Simulations with CHIMERA code show faster and more energetic explosions. Onset of explosion at essentially the same time for different progenitors (?)

### Relativistic 2D SN Models: 11.2 and 15 M Stars



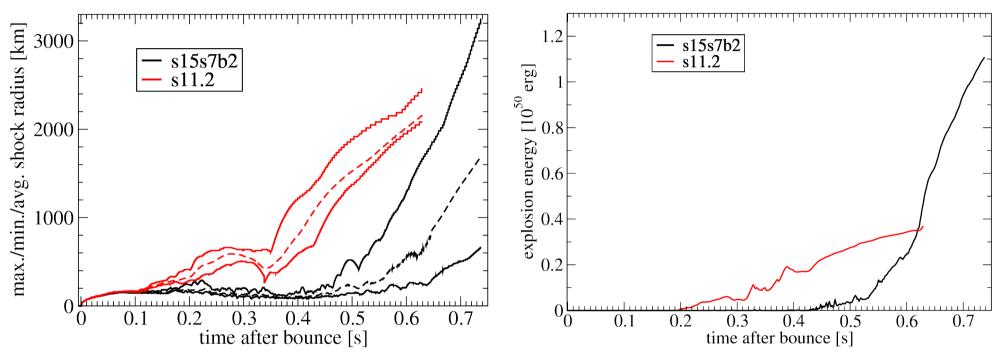
Violent, long lasting shock oscillations produce quasi-periodic variations of neutrino emission and gravitationalwave signal. (Müller, THJ, Marek & Dimmelmeier, to be submitted)



### Relativistic 2D SN Simulations

#### Shock radii

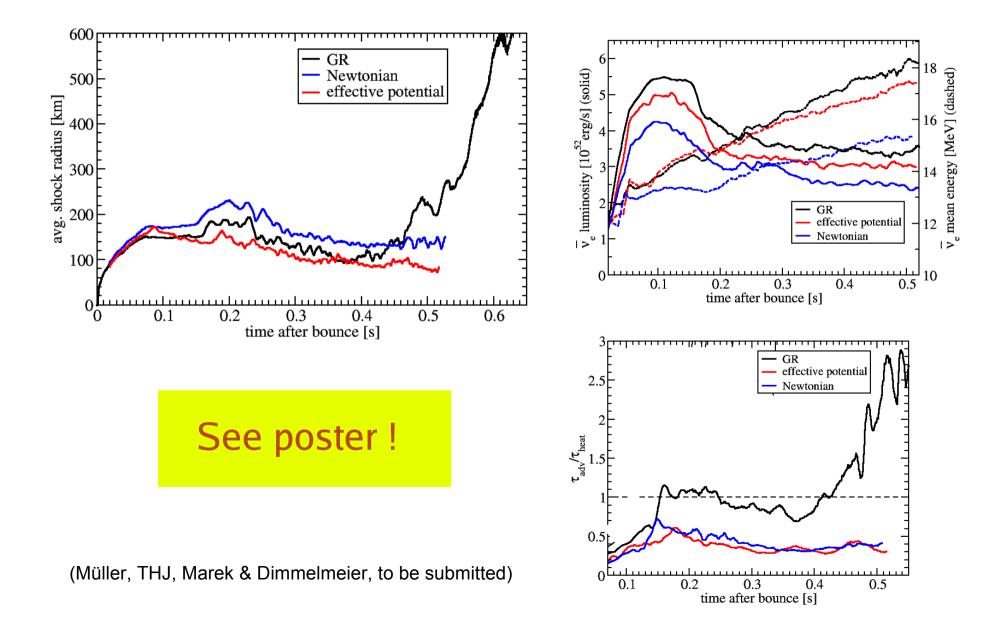
#### **Explosion energies**



(Müller, THJ, Marek & Dimmelmeier, to be submitted)

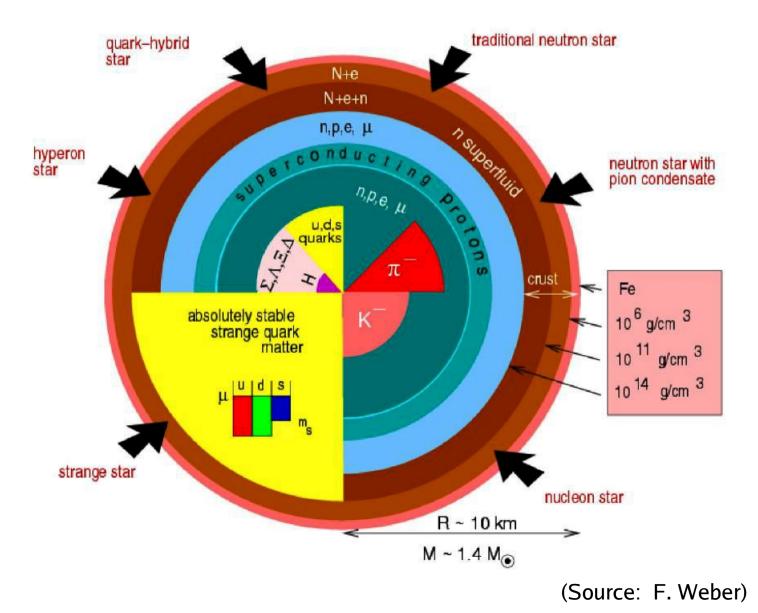
- Relativistic (GR) 2D calculations basically confirm our "post-Newtonian" results.
- Explosions with GR develop somewhat faster and earlier. GR effects help!
- 2D explosions are seemingly "marginal", i.e., tend to set in late and to be relatively weak and highly deformed.

#### General Relativity Fosters Explosions

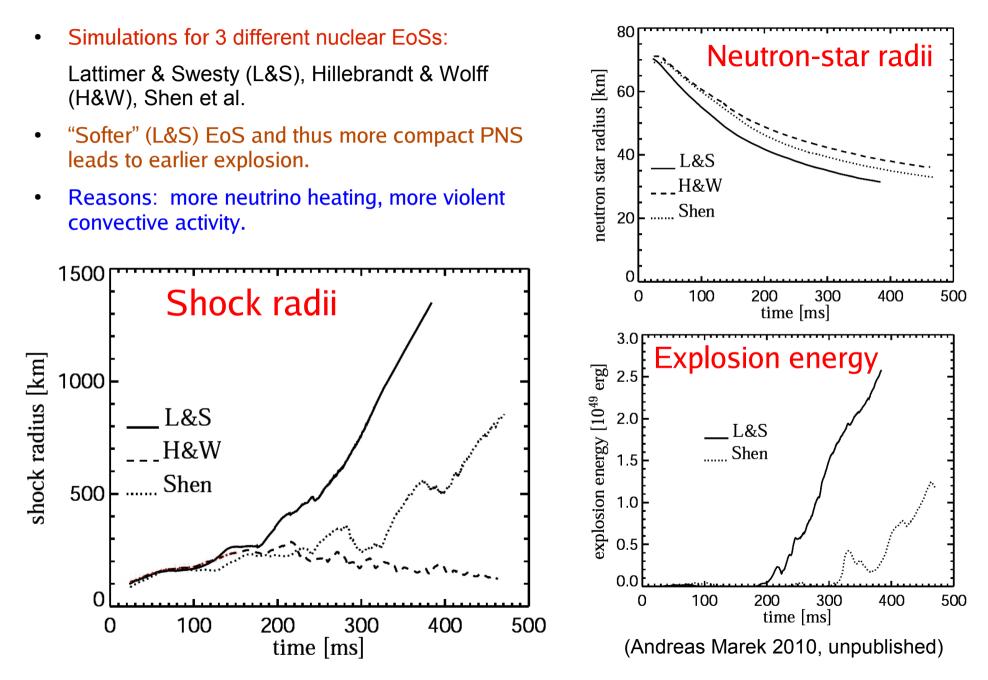


#### Neutron Star Equations of State

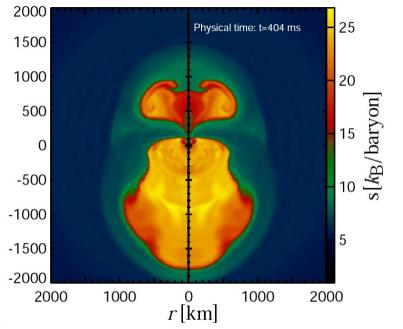
Neutron star EoS is crucial ingredient but highly uncertain!



#### 2D Explosions of 11.2 $M_{sun}$ star : Test of EoS Influence

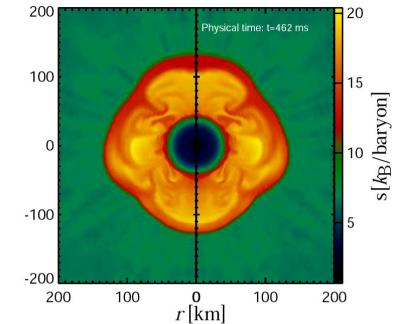


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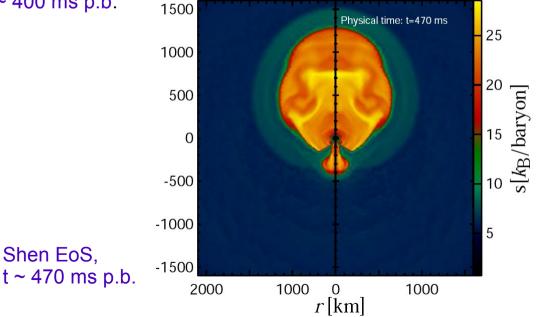


Shen EoS,





H&W EoS, t ~ 460 ms p.b.



(Andreas Marek 2010, unpublished)

## 3D vs. 2D Differences ?

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#### DIMENSION AS A KEY TO THE NEUTRINO MECHANISM OF CORE-COLLAPSE SUPERNOVA EXPLOSIONS

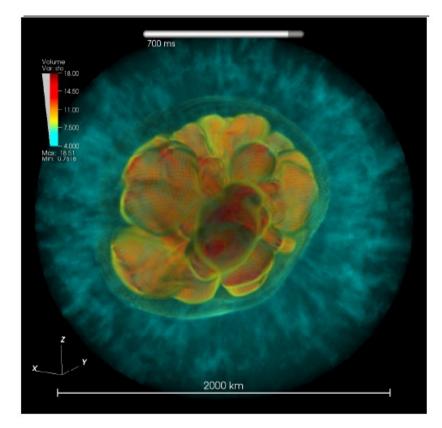
J. NORDHAUS<sup>1</sup>, A. BURROWS<sup>1</sup>, A. ALMGREN<sup>2</sup>, AND J. BELL<sup>2</sup>

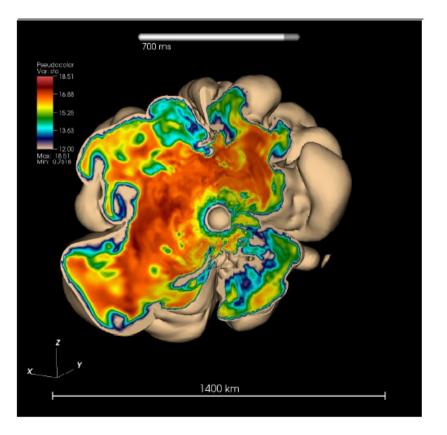
<sup>1</sup> Department of Astrophysical Sciences, Princeton University, Princeton, NJ 08544, USA; nordhaus@astro.princeton.edu, burrows@astro.princeton.edu <sup>2</sup> Computational Research Division, Lawrence Berkeley National Lab, Berkeley, CA 94720, USA; ASAImgren@lbl.gov, JBBell@lbl.gov Received 2010 June 18; accepted 2010 July 7; published 2010 August 12

> However, the difference in the character of 3D turbulence, with its extra degree of freedom and inverse cascade to smaller turbule scales than are found in 2D, may further increase the time matter spends in the gain region, so that the critical condition for explosion (Burrows & Goshy 1993; Murphy & Burrows 2008) is more easily achieved. Our thesis in embarking upon this project was that if going from 2D to 3D improves prospects for the neutrino-driven explosion by the same degree as already demonstrated by going from 1D to 2D (see Section 2), then the neutrino-driven mechanism would perhaps be shown to be not only viable, but also robust. In that case, the details of neutrino interactions, general relativity, and nuclear physics would be of secondary importance for demonstrating the mechanism of explosion,

### 3D Supernova Simulations are Needed!

- 3D code version is presently constructed and in test phase (F. Hanke, L. Hüdepohl, B. Müller; Andreas Marek (RZG)).
- We are beginning to explore 3D phenomena and effects (F. Hanke).





Simulations: Florian Hanke; Visualization: Elena Erastova, Markus Rampp (RZG)

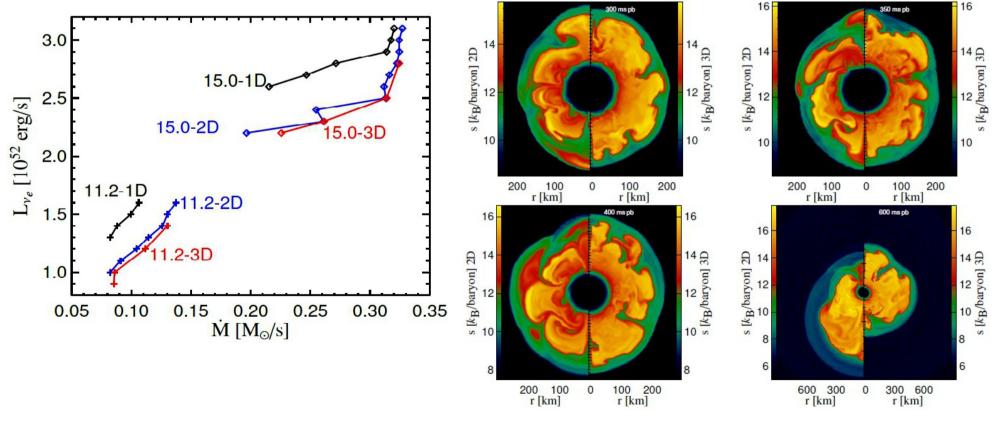
### 2D-3D Differences in Parametric Explosion Models

 Nordhaus, Burrows et al. performed 2D & 3D simulations with simple neutrinoheating and cooling terms and found 15-25% improvement in 3D for 15 M<sub>sun</sub> progenitor star (ApJ 720 (2010) 694)

$$\mathcal{H} = 1.544 \times 10^{20} \left( \frac{L_{\nu_{e}}}{10^{52} \text{ erg s}^{-1}} \right) \left( \frac{T_{\nu_{e}}}{4 \text{ MeV}} \right)^{2} \qquad \mathcal{C} = 1.399 \times 10^{20} \left( \frac{T}{2 \text{ MeV}} \right)^{6} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \times \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} (Y_{n} + Y_{p}) e^{-\tau_{\nu_{e}}} \left[ \frac{\text{erg}}{\text{g s}} \right] \\ \frac{32}{9} \left( \frac{100 \text{ km}}{r} \right)^{2} \left( \frac$$

### 2D-3D Differences in Parametric Explosion Models

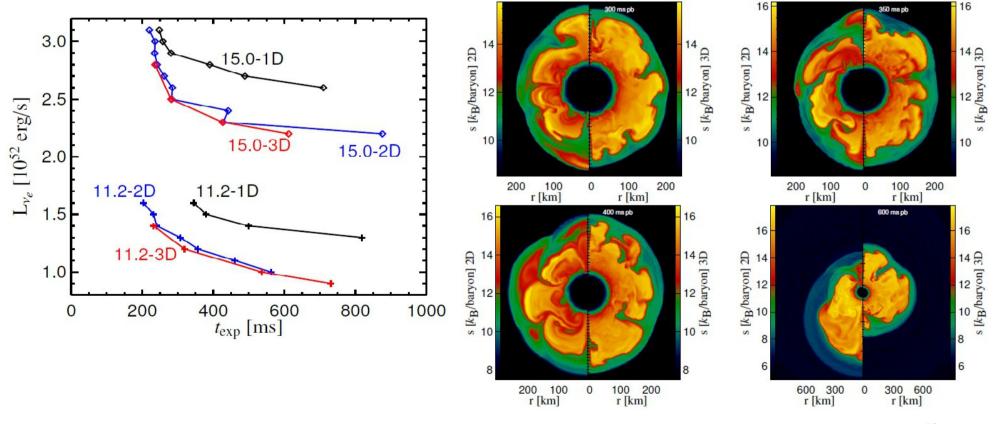
 F. Hanke (Diploma Thesis, MPA, Garching, 2010) in agreement with L. Scheck (PhD Thesis, MPA, 2007) cannot confirm the findings by Nordhaus et al. (2010) ! 2D and 3D simulations for 11.2 M<sub>sun</sub> and 15 M<sub>sun</sub> progenitors are very similar!



2D & 3D slices for 11.2  $M_{sun}$  model, L = 1.0\*10<sup>52</sup> erg/s

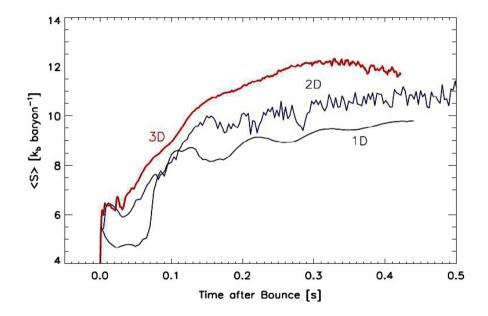
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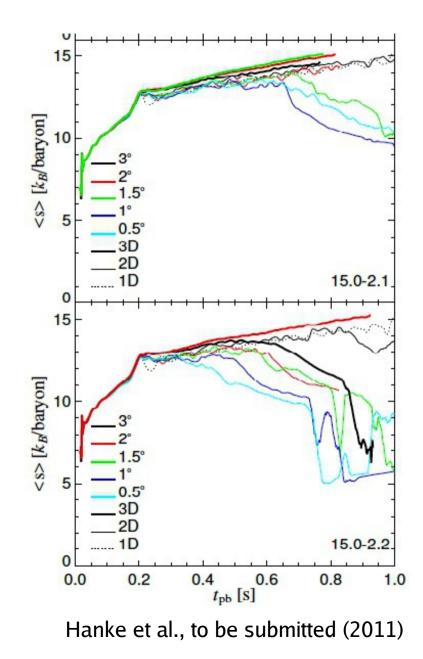


2D & 3D slices for 11.2  $M_{sun}$  model, L = 1.0\*10<sup>52</sup> erg/s

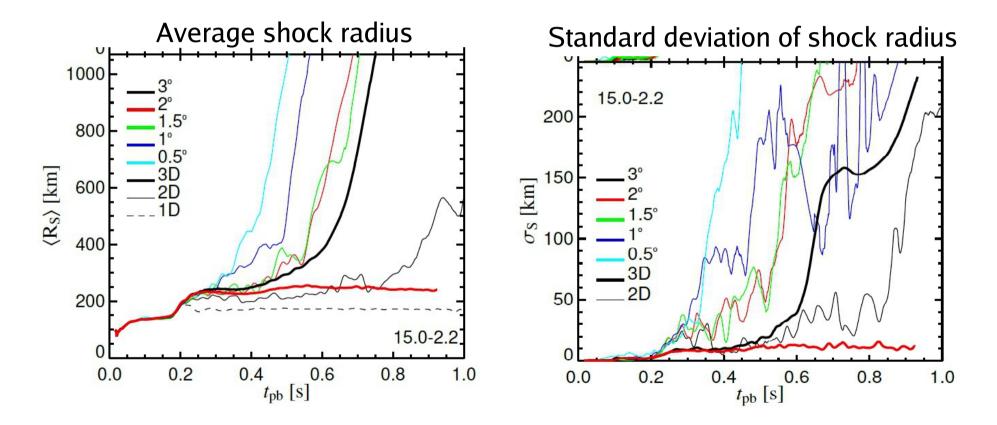
#### Average entropy of gas in gain layer is not good diagnostic quantity for proximity to explosion



Nordhaus et al., ApJ (2010)

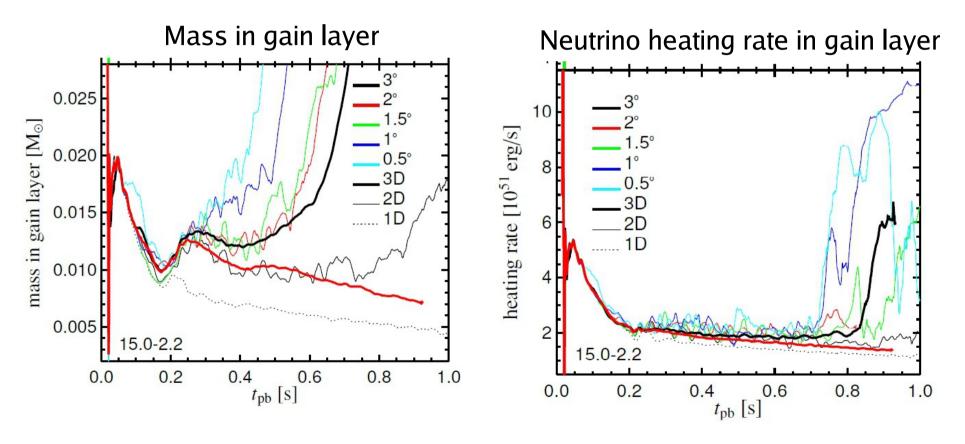


# Higher angular resolution fosters explosions in 2D but delays or prevents explosions in 3D !!!



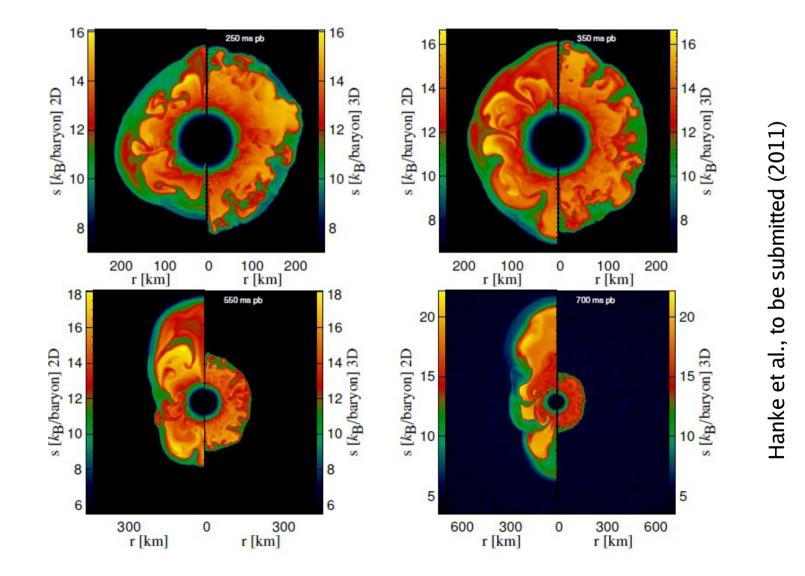
Hanke et al., to be submitted (2011)

# 3D models with higher angular resolution become more similar to 1D models !!!



Hanke et al., to be submitted (2011)

Turbulent energy cascade in 2D "powers" SASI, but in 3D drives small-scale vortex flows and fragmentation



# Questions & Challenges

- OF COURSE, 3D IS IMPORTANT!
- 2D-3D difference depends on neutrino treatment. Detailed transport will be necessary to clarify 3D effects!
- Findings by Nordhaus et al. are NOT "robust".
- We find evidence that turbulent energy cascade fosters SASI in 2D with higher resolution, but to damp it in 3D
- Large-scale mass motions improve explosion conditions, enhanced turbulence on small scales does not in our simulations!
- Is 3D hydrodynamics more favorable for explosions than 2D? The answer is not clear yet!!
- What could stir SASI in 3D? Better neutrino physics? Stellar rotation to seed spiral modes? Progenitor anisotropies/perturbations?
- We need detailed comparisons of physics and numerics between different groups!